MATHEMATICS

Department of Mathematics College of Natural Science

100E Intermediate Algebra Workshop for the Mathematics Enrichment Program Fall, Spring. 1(0-4) R: Approval of department. C: MTH 1825 concurrently.

MTH

Enrichment topics in intermediate algebra for students in the Mathematics Enrichment Program.

103 College Algebra

Fall, Spring, Summer. 3(3-0) P: (MTH 1825) or designated score on Mathematics Placement test SA: LBS 117 Not open to students with credit in MTH 116.

Number systems; functions and relations; exponents and logarithms; elementary theory of equations; inequalities; and systems of equations.

College Algebra Workshop for the 103E

Mathematics Enrichment Program Fall, Spring. 1(0-4) R: Approval of department. C: MTH 103 concurrently.

Enrichment topics in college algebra for students in the Mathematics Enrichment Program.

110 Finite Mathematics and Elements of College Algebra

Fall, Spring, Summer. 5(5-0) P: (MTH 1825) or designated score on Mathematics Placement test Not open to students with credit in MTH 112.

Functions and graphs. Equations and inequalities. Systems of equations. Matrices. Linear programming. Simplex algorithm. Probability and statistics.

Finite Mathematics and Elements of College Algebra for Mathematics 110E Enrichment

Spring. 1(0-2) R: Approval of department. C: MTH 110 concurrently.

Enrichment topics in finite mathematics and elements of college algebra.

112 Finite Mathematics: Applications of College Algebra

Fall, Spring, Summer. 3(3-0) P: (MTH 103) or designated score on Mathematics Placement test SA: MTH 106 Not open to students with credit in MTH 110.

Combinatorics, probability and statistics, mathematics of finance, geometry, transition matrices, and linear programming. The course emphasizes appli-cations and includes work using spreadsheets.

114 Trigonometry

Fall, Spring, Summer. 3(3-0) P: MTH 103 SA: MTH 104 Not open to students with credit in MTH 116.

Radian and degree measure of angles. Definitions and graphs of trigonometric functions and their inverses. Solving trigonometric equations. Applications including identities, indirect measurement and trigonometric modeling.

116 **College Algebra and Trigonometry**

Fall, Spring, Summer. 5(5-0) P: (MTH 1825) or designated score on Mathematics Placement test SA: LBS 117 Not open to students with credit in MTH 103.

Functions and graphs. Equations and inequalities. Exponential and logarithmic functions. Trigonometric functions. Systems of equations. Binomial theorem.

116E Precalculus Workshop for the Emerging Scholars Program

Fall. 1(0-4) R: Approval of department. C: MTH 116 concurrently.

Enrichment topics in precalculus for students in the Emerging Scholars Program.

Survey of Calculus I 124

Fall, Spring, Summer. 3(3-0) P: (MTH 103 or MTH 116) or designated score on Mathematics Placement test Not open to students with credit in LB 118 or MTH 132 or MTH 152H.

Study of limits, continuous functions, derivatives. integrals and their applications.

Survey of Calculus with Applications I 124E Mathematics Enrichment Workshop Fall. 1(0-4) R: Approval of department. C:

MTH 124 concurrently. Enrichment topics in Survey of Calculus with Appli-

cations I for students in the Mathematics Enrichment Program.

126 Survey of Calculus II

Fall, Spring, Summer. 3(3-0) P: MTH 124 Not open to students with credit in MTH 133 or MTH 153H.

Application of partial derivatives, integrals, optimization of functions of several variables and differential equations.

132 Calculus I

Fall, Spring, Summer. 3(3-0) P: (MTH 103 and MTH 114) or (MTH 116 or designated score on Mathematics Placement test) Not open to students with credit in LB 118 or MTH 152H

Limits, continuous functions, derivatives and their applications. Integrals and the fundamental theorem of calculus.

132E Calculus I Workshop for the Emerging Scholars Program

Fall, Spring. 2(0-6) R: Approval of depart-ment. C: MTH 132 concurrently.

Enrichment topics in Calculus I for students in the Emerging Scholars Program.

133 Calculus II

Fall, Spring, Summer. 4(4-0) P: MTH 132 or MTH 152H or LB 118 Not open to students with credit in LB 119 or MTH 153H.

Applications of the integral and methods of integration. Improper integrals. Polar coordinates and parametric curves. Sequences and series. Power series.

133E Calculus II Workshop for the Emerging Scholars Program

Fall, Spring. 1(0-4) R: Approval of depart-ment. C: MTH 133 concurrently. Enrichment topics in Calculus II for students in the

Emerging Scholars Program.

152H Honors Calculus I

Fall. 3(3-0) R: Open to students in the Honors College or approval of department. Not open to students with credit in LB 118 or MTH 132.

Limits, continuous functions, derivatives, integrals, fundamental theorem of calculus. Special emphasis on concepts and theory.

153H Honors Calculus II

Fall, Spring. 4 credits. P: MTH 152H or MTH 132 or LB 118 R: Open to students in the Honors College or approval of department. Not open to students with credit in LB 119 or MTH 133.

The integral. Improper integrals. Polar coordinates and parametric curves. Sequences and series. Power and Taylor series. Special emphasis on concepts and theory.

1825 Intermediate Algebra

Fall, Spring, Summer. 3(3-0) Properties of real numbers. Factoring. Roots and radicals. First and second degree equations. Linear inequalities. Polynomials. Systems of equations.

201 Elementary Mathematics for Teachers I

Fall, Spring, Summer. 3(3-0) P: (MTH 103 or MTH 110 or MTH 116 or MTH 124 or MTH 132 or MTH 152H or LB 118) or designated score on Mathematics Placement test R: Open to students in the Child Development major or in the Education major or in the Special Education-Deaf Education major or in the Special Education-Learning Disabilities major or in the Teacher Certification Internship Year Studies Program.

Mathematics needed for K-8 teaching. Place value and models for arithmetic, mental math, word problems, and algorithms. Factors, primes, proofs, and prealgebra. Fractions, ratios, rates, and percentages. Negative, rational, and real numbers. Special emphasis on the appropriate sequential order for teaching.

202

Elementary Mathematics for Teachers II Fall, Spring, Summer. 3(3-0) P: MTH 201 R: Open to students in the Child Development major or in the Education major or in the Special Education-Deaf Education major or in the Special Education-Learning Disabilities major or in the Teacher Certification Internship Year Studies Program.

A continuation of MTH 201. Geometry, measurement, and elementary data analysis.

Multivariable Calculus 234

Fall, Spring, Summer. 4(4-0) P: MTH 133 or MTH 153H or LB 119 Not open to students with credit in MTH 254H or LB 220.

Vectors in space. Functions of several variables and partial differentiation. Multiple integrals. Line and surface integrals. Green's and Stokes's theorems.

235

Differential Equations Fall, Spring, Summer. 3(4-0) P: MTH 234 or MTH 254H or LB 220 R: Not open to students in the Department of Mathematics or in the Lyman Briggs Computational Mathematics Coordinate Major or in the Lyman Briggs Mathematics Coordinate Major. Not open to students with credit in MTH 255H.

Separable and exact equations. Linear equations and variation of parameters. Higher order linear equations. Laplace transforms. Systems of firstorder linear equations. Introduction to partial differential equations and Fourier series.

254H Honors Multivariable Calculus

Fall, Spring. 4 credits. P: MTH 153H or MTH 133 or LB 119 R: Open to students in the Honors College or approval of depart-ment. Not open to students with credit in LB 220 or MTH 234

Vectors in space. Functions of several variables and partial differentiation. Multiple integrals. Line and surface integrals. Green's and Stokes's Theorems.

255H **Honors Differential Equations**

Fall, Spring. 3(3-0) P: MTH 254H R: Not open to students in the Bachelor of Arts in Mathematics or Bachelor of Science in Mathematics or Lyman Briggs School Mathematics coordinate majors. Not open to students with credit in MTH 235.

Topics chosen from separable and exact equations, linear equations and variation of parameters, series solutions, higher order linear equations, Laplace transforms, systems of first-order linear equations. nonlinear equations and stability, introduction to partial differential equations.

Directed Study 290

Fall, Spring, Summer. 1 to 4 credits. A student may earn a maximum of 6 credits in all enrollments for this course.

Faculty directed study of selected mathematical topics.

291 **Mathematics Snapshots**

Spring. 1(2-0) A student may earn a maximum of 2 credits in all enrollments for this course. P: MTH 116 or approval of department

Selected topics in mathematics and its applications. Emphasis will be on important and intriguing ideas in mathematics without indulging in technical details.

299 Transitions

Fall, Spring, Summer. 4 credits. P: MTH 132 or LB 118 RB: (MTH 133 or concurrently) or (LB 119 or concurrently)

Introduction to mathematical reasoning, basic logic, set theory, integers, natural numbers and induction, basic number theory, real numbers, limits, sequences, series.

301 Foundations of Higher Mathematics

Fall, Spring. 3(3-0) P: MTH 133 or MTH 153H or LB 119

Elementary set theory including permutations, com-binations, cardinality theorems, relations, functions and quotient sets. Basic principles of logic and proof techniques. Elementary number theory and abstract algebra.

304 Algebra for Elementary and Middle School Teachers

Fall. 3 credits. Interdepartmental with Teacher Education. Administered by Mathematics. P: (MTH 201 and MTH 202 and MTH 301) and completion of Tier I writing requirement R: Open to undergraduate students in the College of Education or in the Department of Teacher Education. Approval of department.

Algebra needed for understanding connections between topics of algebra and the mathematics taught in elementary and middle school.

Functions and Calculus for Elementary 305 and Middle School Teachers (W)

Spring. 3 credits. Interdepartmental with Teacher Education. Administered by Mathematics. P: MTH 304

Functions and calculus needed for understanding connections between topics of calculus and the mathematics taught in middle school.

309 Linear Algebra I

Fall, Spring, Summer. 3(3-0) P: ((MTH 133 or MTH 153H or LB 119) and completion of Tier I writing requirement) and (MTH 299 or approval of department)

Matrices, systems of linear equations, vector spaces, linear transformations, inner products and orthogonal spaces, eigenvalues and eigenvectors, and applications to geometry. A writing course with emphasis on proofs.

310

Abstract Algebra I and Number Theory Fall, Spring, Summer. 3(3-0) P: ((MTH 299 or MTH 317H)or approval of department) and completion of Tier I writing requirement Structure of the integers, congruences, rings, ring homomorphisms, ideals, quotient rings. A writing course with an emphasis on proofs.

314 Matrix Algebra with Applications

Fall, Spring, Summer. 3(3-0) P: MTH 234 or MTH 254H or LB 220 R: Not open to students in the Department of Mathematics or in the Lyman Briggs Computational Mathematics Coordinate Major or in the Lyman Briggs Mathematics Coordinate Major.

Problem-solving and applications in matrix algebra for scientists and engineers. Vectors, matrices, linear transformations, inner products, dimension, eigenvalues and eigenvectors. Applications to systems of equations and to geometry.

Honors Linear Algebra 317H

Fall, Spring. 4 credits. P: MTH 133 or MTH 153H or LB 119 R: Open to students in the

Honors College or approval of department. Systems of equations, matrix algebra, vector spaces, linear transformations, geometry of R^n, eigenvalues, eigenvectors, diagonalization, inner products. Emphasis on mathematical reasoning, proofs, and concepts.

320 Analysis I

Fall, Spring, Summer. 3(3-0) P: (MTH 133 or MTH 153H or LB 119) and (MTH 299 or MTH 317H or approval of department) Not open to students with credit in MTH 327H.

Convergence of sequences and series. Upper and lower limits, completeness, limits and continuity. Derivatives. Uniform convergence.

327H Honors Introduction to Analysis

Fall, Spring. 3(3-0) P: MTH 317H R: Approval of department. Not open to students with credit in MTH 320.

Emphasis on foundations and metric topology. Convergence of sequence and series, continuity of functions. Differentiation and integration in one dimension.

330 **Higher Geometry**

Fall, Spring, Summer. 3(3-0) P: MTH 301 or MTH 309 or MTH 299 or MTH 317H

Topics in transformations: isometries, similarities, inversion. Advanced Euclidean geometry: theorems of Menelaus, Ceva, and Desargues. Cross ratio, harmonic points, analytic, metric, and vector methods, and convexity.

Ordinary Differential Equations I 340

Fall, Spring, Summer. 3(3-0) P: MTH 309 Techniques for solving differential equations, existence and uniqueness theorems, qualitative theory. Fourier series and applications.

347H Advanced Ordinary Differential Equations

Spring. 3(3-0) P: MTH 317H R: Approval of department.

Separable and exact equations, linear equations and variation of parameters, higher order linear equations, Laplace Transforms, first-order linear classification of singularities, nonlinear systems, systems, partial differential equations and Fourier Series, existence and uniqueness theorems. There will be an emphasis on theory.

Theory of Mathematical Interest 360

Fall, Spring. 3(3-0) P: (MTH 234 or concur-rently) or (MTH 254H or concurrently) or (LB 220 or concurrently) or approval of department

Measurement of interest rates, basic problems in interest theory, basic annuities, continuous and varying annuities, yield rates, amortization, bonds and other securities, practical applications, and stochastic approaches to interest.

370 Mathematical Biology

Fall. 3(3-0) P: (MTH 133 or LB 119) and (BS 161 or BS 162 or BS 181H or BS 182H or LB 144 or LB 145)

First-order linear ordinary differential equations and systems. Qualitative theory of nonlinear continuous dynamical systems. Reaction-diffusion equations. Numerical analysis and computer simulation of solutions to nonlinear systems of differential equations. Numerical linear algebra. Applications to biological sciences.

Statistical Biology 371

Spring. 3(3-0) Interdepartmental with Statistics and Probability. Administered by Statis-tics and Probability. P: (MTH 132 or LB 118 or approval of department) and (STT 231 or STT 351 or STT 421 or STT 441 or STT 464 or approval of department) and (BS 161 or BS 162 or BS 181H or BS 182H or LB 144 or LB 145)

Probability models in biological systems. Design and analysis of biological experiments including ANOVA models. Multiple testing. Classification and clustering for genomic and proteomic data. Computational software packages. Internet-based query systems.

Capstone in Mathematics for Secondary 396 Education (W)

Spring. 3(3-0) P: ((MTH 309 and MTH 310 and MTH 320)or approval of department) and completion of Tier I writing requirement R: Approval of department. Not open to students with credit in MTH 496.

A capstone course for secondary education math majors. High school mathematics from an advanced viewpoint.

411 Abstract Algebra II

Fall, Spring. 3(3-0) P: MTH 310 Not open to students with credit in MTH 418H.

Continuation of MTH 310. Permutation groups, groups of transformations, normal subgroups, homomorphism theorems, modules. Principal ideal rings, unique factorization domains, noncommutative rings, rings of fractions, ideals.

414 Linear Algebra II

Fall. 3(3-0) P: MTH 309 or MTH 314 Not open to students with credit in MTH 415. Linear transformations on finite dimensional vector spaces. Invariant subspaces, rank, eigenvalues and eigenvectors. Canonical forms. Bilinear and multilinear forms.

415 Applied Linear Algebra

Fall, Spring, Summer. 3(3-0) P: (MTH 235 or MTH 255H or MTH 340) and (MTH 309 or MTH 314) Not open to students with credit in MTH 414.

Matrices and linear algebra. General linear systems of equations. Least squares minimization techniques. Eigenvalues and eigenvectors, spectral decompositions, and exponentials.

416 Introduction to Algebraic Coding Fall. 3(3-0) P: MTH 309

Concepts and techniques of abstract algebra ap-plied to the design of communication systems for use in imperfect circumstances. Theory of codes designed by algebraic means.

417 **Topics in Number Theory**

Spring of even years. 3(3-0) P: MTH 310 Congruences of higher degree, primitive roots and quadratic reciprocity. Number-theoretic functions, algebraic numbers. Dirichlet Series, p-order expansion, continued fractions.

418H Honors Algebra I

Fall. 3(3-0) P: Completion of Tier I writing requirement. RB: MTH 309 R: Approval of department. Not open to students with credit in MTH 411.

Theory of groups, Sylow theory, the structure of finite Abelian groups, ring theory, ideals, homomor-phisms, and polynomial rings.

419H Honors Algebra II

Spring. 3(3-0) P: MTH 418H R: Approval of department.

Algebraic field extensions, Galois theory. Classification of finite fields. Fundamental Theorem of Algebra.

421 Analysis II

Fall, Spring. 3(3-0) P: (MTH 320 or MTH 327H) and (MTH 234 or MTH 254H or LB 220)

Continuation of MTH 320. Riemann integral. Metric spaces. Differentiation in higher dimensions. Inverse and implicit function theorems.

Complex Analysis 425

Fall, Spring. 3(3-0) P: MTH 320

Analytic functions of a complex variable, Cauchy integral theorem, conformal maps, bilinear transformation, harmonic functions, Classification of singularities, residues, conformal mappings.

428H

Honors Complex Analysis Fall. 3(3-0) P: MTH 327H R: Approval of department.

Analytic functions of a complex variable, line integrals and harmonic functions, Cauchy's theorem and integral formula, power series, Laurent series, isolated singularities, residue calculus, Rouche's theorem, automorphisms of the disk, the Riemann mapping theorem.

429H **Honors Real Analysis**

Spring. 3(3-0) P: MTH 327H R: Approval of department. Not open to students with credit in MTH 421

Continuation of 327H. Convergence of sequences and series of functions, differentiation and integration in higher dimensional settings. Inverse and implicit function theorems.

432 **Axiomatic Geometry**

Spring. 3(3-0) P: MTH 309

Axiomatic systems and finite geometries: axioms of Euclidean and hyperbolic geometry, the Poincare model, independence of the parallel postulate. Classical constructions and the impossibility of angle trisection

441 **Ordinary Differential Equations II**

Fall. 3(3-0) P: (MTH 235 or MTH 255H or MTH 340 or MTH 347H) and (MTH 309 or MTH 317H or MTH 314 or MTH 415)

Existence and uniqueness theorems; Linearization; Local and global stability; Saddle-node, Hopf and heteroclinic bifurcations; Hamiltonian and gradient system; The Poincare map; The Poincare-Bendixson theorem and limit cycles; Selected applications.

442 **Partial Differential Equations**

Spring. 3(3-0) P: MTH 235 or MTH 255H or MTH 340 or MTH 347H

Classification of second order partial differential equations. Boundary and initial value problems for heat, Laplace, and wave equations in dimensions 1, 2 and 3. Variational methods and maximum principles. Separation of variables, Fourier series, Sturm-Liouville theory. Greens functions.

Boundary Value Problems for Engineers 443 Fall. 3(3-0) P: MTH 235 or MTH 255H R: Not open to students in the Department of Mathematics

Fourier series and orthogonal functions. Method of separation of variables for partial differential equations. Sturm-Liouville problems.

451 Numerical Analysis I

Fall. 3(3-0) P: (CSE 131 or CSE 231) and (MTH 309 or MTH 314 or MTH 317H or MTH 415) and (MTH 235 or MTH 255H or MTH 340 or MTH 347H) SA: MTH 351

Numerical solution of linear and nonlinear algebraic equations and eigenvalue problems. Curve fitting. Interpolation theory. Numerical integration, differentiation, and solution of differential equations. Algorithms implementation with a programming language like Fortran, C/C++ or MATLAB.

Numerical Analysis II Spring. 3(3-0) P: MTH 451 452

Iterative methods for solving linear systems, approximation theory, approximating eigenvalues, solutions of systems of nonlinear equations, boundary-value problems for ordinary differential equations, numerical methods for partial differential equations.

Actuarial Models I 455

Fall. 3(3-0) Interdepartmental with Statistics and Probability. Administered by Statistics

and Probability. RB: STT 441 and MTH 360 Stochastic models used in insurance. Survival distributions, life insurance, life annuities, benefit premiums, benefit reserves, and analysis of benefit reserves.

456 Actuarial Models II

Spring. 3(3-0) Interdepartmental with Statistics and Probability. Administered by Statistics and Probability. P: STT 455 Continuation of STT 455. Benefit reserves. Multiple

life functions. Multiple decrement models and their applications. Elements of stochastic processes for actuaries including Markov chains and Poisson processes

457 Introduction to Financial Mathematics Spring. 3(3-0) P: MTH 309 and (MTH 340 or

MTH 235 or MTH 255H) and (STT 441 or STT 351) Mathematical overview of basic financial instru-

ments. A unified partial differential equation approach to model derivative securities. Partial differential equations in financial mathematics, Black-Scholes equation. Numerical methods for valuing derivatives

458 **Financial Mathematics for Actuaries**

Fall. 3(3-0) Interdepartmental with Statistics and Probability. Administered by Mathemat-ics. P: MTH 360 and STT 441 and FI 379

Evaluate and construct interest rate models. Rational valuation of derivative securities using put-call parity and calculation of European and American options. Risk management techniques using the method of delta-hedging.

459 **Construction and Evaluation of Actuarial** Models

Spring. 3(3-0) Interdepartmental with Statistics and Probability. Administered by Statistics and Probability. P: STT 442

Severity, frequency, and aggregate models. Construction of empirical models. Parametric statistical methods. Credibility analysis. Simulation methods.

461 Metric and Topological Spaces

Fall. 3(3-0) P: MTH 320 or MTH 428H Set theory, metric spaces, topological spaces, maps, product and quotient topologies. Connected and compact spaces, separation axioms, pointwise and uniform convergence.

481 **Discrete Mathematics I**

Fall, Spring. 3(3-0) P: MTH 309 Binomial and multinomial theorems. Graphs and digraphs, graph coloring. Generating functions, asymptotic analysis, trees. Representing graphs in computers.

482 **Discrete Mathematics II**

Spring. 3(3-0) P: MTH 481 RB: MTH 310 Recurrence and generating functions, Ramsey theory. Block designs, Latin squares, Eulerian and Hamiltonian paths. Minimum spanning trees, network flows.

490 **Directed Studies**

Fall, Spring, Summer. 1 to 4 credits. A student may earn a maximum of 9 credits in all enrollments for this course. R: Approval of department.

Faculty directed study in a selected mathematical topic.

491A

Actuarial Internship Summer. 3(3-0) RB: STT 441 and FI 311 and MTH 360 R: Approval of department.

Survey of typical actuarial type projects at an actuarial firm such as data analysis, risk analysis, interest rate models, life insurance, benefit programming, analysis of benefit reserves.

491B **Teamwork Experience**

Fall, Spring. 1(1-0) R: Approval of department

A field type experience to develop communication skills working in a group setting on multi-faceted projects.

496 **Capstone in Mathematics**

Fall, Spring. 3(3-0) P: Completion of Tier I writing requirement. R: Approval of department.

A capstone course integrating several areas of mathematics.

810 **Error-Correcting Codes**

Spring. 3(3-0) RB: MTH 411 or MTH 414 or MTH 415

Block codes, maximum likelihood decoding, Shannon's theorem. Generalized Reed-Solomon codes, modification of codes, subfield codes. Alterant and Goppa codes, cyclic codes and BCH codes.

818 Algebra I

Fall. 3(3-0) RB: MTH 411 Group theory: Sylow theory, permutation groups, Jordon-Hoelder theory, Abelian groups, free groups. Ring theory: algebra of ideals, unique factorization, polynomial rings, finitely generated modules over PIDs.

819 Algebra II

Spring. 3(3-0) RB: MTH 818

Modules and vector spaces, projectives modules, tensor algebra. Fields and Galois groups, algebraic and transcendental numbers, non-commutative rings. The Jacobson radical, the structure of semisimple rings with the descending chain condition.

828 Real Analysis I

Fall. 3(3-0) RB: MTH 421 and MTH 461 Lebesque measure on real line, general measure theory. Convergence theorems, Lusin's theorem, Egorov's theorem, Lp-spaces, Fubini's theorem. Functions of bounded variation, absolutely continuous functions, Lebesgue differentiation theorem.

829 Complex Analysis I

Spring. 3(3-0) RB: MTH 421 and MTH 425 Cauchy theorem, identity principle, Liouville's theorem, maximum modulus theorem. Cauchy formula, residue theorem, Rouche's theorem. Casorati-Weierstrass theorem, Arzela-Ascoli theorem. Conformal mapping, Schwarz lemma, Riemann mapping theorem.

840 **Chaos and Dynamical Systems**

Spring. 3(3-0) RB: (MTH 441 and MTH 320 and MTH 414) and some experience with mathematical software such as Mathematica or Matlab.

Chaotic or random motions in differential and difference equations.

841

Boundary Value Problems I Fall. 3(3-0) RB: MTH 414 and MTH 421 Methods for solving boundary and initial value problems for ordinary and partial differential equations.

Boundary Value Problems II 842

Spring. 3(3-0) RB: MTH 841 Continuation of MTH 841.

Survey of Industrial Mathematics 843

Fall. 3(3-0) RB: ((MTH 414 or MTH 415) or Some familiarity with mathematical software such as Mathematica, Matlab, etc.) and (MTH 421 and MTH 442) R: Open only to masters students in the Industrial Mathematics major or approval of department.

Fundamentals of mathematical modeling in government and industry, including modes of industrial communication.

844 **Projects in Industrial Mathematics**

Spring. 3(3-0) RB: ((MTH 414 or MTH 415) or some familiarity with mathematical software such as Mathematica or Matlab.) and (MTH 421 and MTH 442 and MTH 843) R: Open only to masters students in the Industrial Mathematics major or approval of department.

Participation as a member of a 3-4 person team on a significant industrial problem, with participation of an industrial liaison, including project report generation and reporting.

Ordinary Differential Equations 848

Fall. 3(3-0) RB: MTH 414 and MTH 421 Existence and uniqueness theorems. Theory of linear differential equations. Floquet theory. Stability theory and Poincare-Bendixson theory. Green's functions and boundary value problems.

849 **Partial Differential Equations**

Spring. 3(3-0) RB: MTH 414 and MTH 421 Cauchy-Kowalewski theorem. Characteristics. Initialboundary value problems for parabolic and hyperbolic equations. Energy methods, boundary value problems for elliptic equations, potential theory. Green's function, maximum principles, Schauder's method.

850 Numerical Analysis I

Fall. 3(3-0) RB: MTH 414 and MTH 421 Convergence and error analysis of numerical methods in applied mathematics.

Numerical Analysis II 851

Fall. 3(3-0) RB: MTH 850 and MTH 852 Spectral methods for boundary value problems, eigenvalue problems, and time-dependent problems. Trigonometric and Chebyshev polynomials. Fast Fourier transforms.

Numerical Methods for Ordinary 852 **Differential Equations** Spring. 3(3-0) RB: MTH 850

Linear multi-step methods and single step nonlinear methods for initial value problems. Consistency, stability and convergence. Finite difference, finite element, shooting methods for boundary value problems.

864

Geometric Topology Spring. 3(3-0) RB: MTH 421 SA: MTH 464 Topology of surfaces and higher dimensional manifolds, studied from combinatorial, algebraic or differential viewpoints.

868 Geometry and Topology I

Fall. 3(3-0) RB: (MTH 411 and MTH 421) or approval of department.

Fundamental group and covering spaces, van Kampen's theorem. Homology theory, Differentiable manifolds, vector bundles, transversality, calculus on manifolds. Differential forms, tensor bundles, deRham theorem, Frobenius theorem.

869 Geometry and Topology II Spring. 3(3-0) RB: MTH 868

Continuation of MTH 868.

879 **Teaching College Mathematics**

Fall of even years. 3(3-0) A student may earn a maximum of 6 credits in all enrollments for this course. Interdepartmental with Counseling, Educational Psychology and Special Education and Mathematics Education and Teacher Education. Administered by Mathematics Education. RB: Past or concurrent mathematics teaching experience. SA: SME 879

Curriculum materials, case studies, approaches to teaching and student learning of particular mathematics topics.

880 Combinatorics

Fall. 3(3-0) RB: MTH 411 or MTH 482 Enumerative combinatorics, recurrence relations, generating functions, asymptotics, applications to graphs, partially ordered sets, generalized Moebius inversions, combinatorial algorithms.

881

Graph Theory Spring. 3(3-0) RB: MTH 880

Graph theory, connectivity, algebraic and topological methods. Networks, graph algorithms, Hamiltonian and Eulerian graphs, extremal graph theory, random graphs

890 **Readings in Mathematics**

Fall, Spring, Summer. 1 to 6 credits. A student may earn a maximum of 24 credits in all enrollments for this course. R: Approval of department.

Individualized study for Master's level students.

Commutative Algebra 910

Fall of odd years. 3(3-0) RB: MTH 819 Noetherian rings and modules, localization and tensor products, primary decomposition, Krull dimensions, graded rings and modules, Hilbert's Nullstellensatz, integral extensions, discrete valuation rings, Dedekind domains.

Commutative Algebra II 911

Spring of even years. 3(3-0) RB: MTH 910 Ext and Tor, regular sequences, Cohen-Macauley rings, regular rings, Gorenstein rings, completion, modules of differentials, Cohen's structure theorems.

Group Theory I 912

Fall of even years. 3(3-0) RB: MTH 819 Permutation groups, solvable and nilpotent groups, simple groups. Representation and character theory. Extension theory and cohomology groups.

Group Theory II 913

Spring of odd years. 3(3-0) RB: MTH 912 Groups of Lie type, linear groups, locally finite groups, free groups and free products, the subgroup theorems.

914 Lie Groups and Algebras

Fall of odd years. 3(3-0) RB: MTH 819 Nilpotent and semisimple algebras, the ad joint representation, root spaces, Weyl groups, Dynkin diagrams, classification of simple algebras.

915 Lie Groups and Algebras II

Spring of even years. 3(3-0) RB: MTH 914 Weights, symmetric spaces, groups of Lie type, finite groups of Lie type, Lang's theorem.

Introduction to Algebraic Geometry I 916 Fall of even years. 3(3-0) RB: MTH 818 and MTH 819

Affine and projective algebraic varieties and their properties. Morphisms and singularities. Schemes and coherent sheaves. Sheaf cohomology and other related topics.

917 Introduction to Algebraic Geometry II Spring of odd years. 3(3-0) RB: MTH 916 Continuation of MTH 916.

918 Number Theory I

Fall of even years. 3(3-0) P: MTH 819 or approval of department

Number fields and algebraic integers, prime ideals and factorization, cyclotomic fields, the class group, the Dirichlet unit theorem, different, discriminant, decomposition and inertia groups, local fields.

919 Number Theory II

Spring of odd years. 3(3-0) P: MTH 918 or approval of department

Topics from: class field theory, zeta and L-functions, modular forms, theory of elliptic curves, diophantine approximation, diophantine geometry.

920 **Functional Analysis I**

Spring. 3(3-0) RB: MTH 828 Hilbert spaces: Riesz representation theorem, Parseval's identity, Riesz-Fisher theorem, Fourier series operators. Banach spaces: Hahn-Banach theorem, open mapping and closed graph theorems, Banach-Steinhaus theorem.

921 Functional Analysis II

Fall of even years. 3(3-0) RB: MTH 829 and MTH 920

Topological vector spaces, convexity, Krein-Milman theorem, Banach algebras, operators on Banach spaces, spectral theorem, C*-algebras.

Harmonic Analysis 922

Fall of odd years. 3(3-0) RB: MTH 829 and MTH 920

Fourier series, mean and pointwise convergence, conjugate functions, Fourier transform, Plancherel theorem, Paley-Wiener theorem, interpolation of operators, Hausdorff-Young thoerem.

926 **Proseminar in Mathematics Education I**

Fall of odd years. 3(3-0) Interdepartmental with Counseling, Educational Psychology and Special Education and Mathematics Education and Teacher Education. Administered by Mathematics Education. SA: SME 926

Research on the learning and teaching of mathematics. Focus on curriculum, discourse, equity and teacher education.

Proseminar in Mathematics Education II 927 Fall of even years. 3(3-0) Interdepartmental with Counseling, Educational Psychology and Special Education and Mathematics Education and Teacher Education. Administered by Mathematics Education. SA: SME 927

Research on the learning and teaching of mathematics. Focus on teaching, student learning, assessment and policy.

928 Real Analysis II

Fall. 3(3-0) RB: MTH 828

Positive Borel measure, complex measures. Riesz representation theorem, Radon-Nikodym theorem, Lebesgue decomposition theorem. Differentiable transformations and change of variables, differentiation of measures, maximal functions.

Complex Analysis II 929

Spring. 3(3-0) RB: MTH 828 and MTH 829 Phragmen-Lindelof method. Hadamard's theorem, Runge's theorem, Weierstrass factorization theorem, Mittag-Leffler theorem, and Picard's theorem. Poisson integrals, Harnack's inequality, Dirichlet problem. Hp-spaces and Blaschke products.

930 **Riemannian Geometry I**

Fall of even years. 3(3-0) RB: MTH 869 Riemannian metrics, connections, curvature, geodesics. First and second variation, Jacobi fields, conjugate points. Rauch comparison theorems, Hodge theorem, Bochner technique, spinors. Further topics on curvature or submanifold theory.

Riemannian Geometry II 931

Spring of odd years. 3(3-0) RB: MTH 930 Continuation of MTH 930.

Complex Manifolds I 935

Fall of odd years. 3(3-0) RB: MTH 829 and MTH 869

Riemann surfaces, Serre duality, Riemann-Roch theorem. Weierstrass points, Abel's theorem, Plucker formulas. Hermitian metrics, connections, curvature, Hodge theorem. Kaehler metrics, Kodaira vanishing theorem, Chern classes.

936 **Complex Manifolds II**

Spring of even years. 3(3-0) RB: MTH 935 Continuation of MTH 935.

940 Applied Analysis I

Fall. 3(3-0) RB: MTH 828 Sobolev spaces, trace theorem, imbedding theo-rems, sectorial forms. Linear elliptic boundary and eigenvalue problems.

Applied Analysis II 941

Spring. 3(3-0) RB: MTH 940 Fixed point theorems. Variational methods. Applications to nonlinear integral and elliptic differential equations. Semigroup theory.

Foundations of Applied Mathematics I 942

Fall. 3(3-0) RB: MTH 848 and MTH 849 Modeling in classical applied mathematics. Newtonian and continuum mechanics. Special mathematical techniques.

Foundations of Applied Mathematics II 943 Spring. 3(3-0) RB: MTH 942

Continuation of MTH 942.

950 Numerical Methods for Partial Differential Equations I

Spring of odd years. 3(3-0) RB: MTH 852 Finite difference methods for ordinary and partial differential equations

951 **Numerical Methods for Partial Differential** Equations II

Spring of even years. 3(3-0)

Finite element methods for ordinary and partial differential equations.

954 **Design and Methods in Mathematics** Education Research

Fall. 3(3-0) Interdepartmental with Counseling, Educational Psychology and Special Education and Mathematics Education and Teacher Education. Administered by Mathematics Education. RB: (MTHE 927) and at least one approved research methods course. SA: SME 954

History, current trends, and issues pertaining to research design and methods in mathematics education research. Mathematics education research in the areas of policy, teaching, teacher learning, and student learning with particular attention to how research design influence research findings.

960 Algebraic Topology I

Fall. 3(3-0) RB: MTH 869

Cohomology, products, duality, basic homotopy theory, bundles, obstruction theory, spectral se-quences, characteristic classes, and other related topics.

961 Algebraic Topology II

Spring. 3(3-0) RB: MTH 960 Continuation of MTH 960.

990 **Reading in Mathematics**

Fall, Spring, Summer. 1 to 3 credits. A student may earn a maximum of 9 credits in all enrollments for this course. R: Approval of department.

Individualized study for doctoral level students.

Special Topics in Algebra 991

Fall, Spring. 3 to 6 credits. A student may earn a maximum of 18 credits in all enrollments for this course. R: Approval of department.

Advanced topics in algebra.

Special Topics in Analysis 992

Fall, Spring. 3 to 6 credits. A student may earn a maximum of 18 credits in all enrollments for this course. R: Approval of department.

Advanced topics in analysis.

993 Special Topics in Geometry

Fall, Spring. 3 to 6 credits. A student may earn a maximum of 18 credits in all enrollments for this course. R: Approval of department.

Advanced topics in geometry.

Special Topics in Applied Mathematics 994

Fall, Spring. 3 to 6 credits. A student may earn a maximum of 24 credits in all enrollments for this course. R: Approval of department.

Advanced topics in applied mathematics.

Special Topics in Numerical Analysis 995 and Operations Research Fall, Spring. 3 to 6 credits. A student may earn a maximum of 18 credits in all enroll-

ments for this course. R: Approval of department. Advanced topics in numerical analysis or operations

research.

996

Special Topics in Topology Fall, Spring. 3 to 6 credits. A student may earn a maximum of 18 credits in all enrollments for this course. R: Approval of department.

Advanced topics in topology

998 Special Topics in Combinatorics and

Graph Theory Fall, Spring. 3 to 6 credits. A student may earn a maximum of 18 credits in all enrollments for this course. R: Approval of department.

Advanced topics in combinatorics and graph theory.

999 **Doctoral Dissertation Research**

Fall, Spring, Summer. 1 to 24 credits. A student may earn a maximum of 36 credits in all enrollments for this course. R: Approval of department.

Doctoral dissertation research.